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Oxidation behavior of FeV_2O_4 and FeCr_2O_4 particles in the air: Nonisothermal kinetic and reaction mechanism

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Abstract: High-temperature oxidation behavior of ferrovandium (FeV_2O_4) and ferrochrome (FeCr_2O_4) spinels is crucial for the application of spinel as an energy material, as well as for the clean usage of high-chromium vanadium slag. Herein, the nonisothermal oxidation behavior of FeV_2O_4 and FeCr_2O_4 prepared by high-temperature solid-state reaction was examined by thermogravimetry and X-ray diffraction (XRD) at heating rates of 5, 10, and 15 K/min. The apparent activation energy was determined by the Kissinger–Akahira–Sunose (KAS) method, whereas the mechanism function was elucidated by the Malek method. Moreover, *in-situ* XRD was conducted to deduce the phase transformation of the oxidation mechanism for FeV_2O_4 and FeCr_2O_4 . The results reveal a gradual increase in the overall apparent activation energies for FeV_2O_4 and FeCr_2O_4 during oxidation. Four stages of the oxidation process are observed based on the oxidation conversion rate of each compound. The oxidation mechanisms of FeV_2O_4 and FeCr_2O_4 are complex and have distinct mechanisms. In particular, the chemical reaction controls the entire oxidation process for FeV_2O_4 , whereas that for FeCr_2O_4 transitions from a three-dimensional diffusion model to a chemical reaction model. According to the *in-situ* XRD results, numerous intermediate products are observed during the oxidation process of both compounds, eventually resulting in the final products FeVO_4 and V_2O_5 for FeV_2O_4 and Fe_2O_3 and Cr_2O_3 for FeCr_2O_4 , respectively.

Keywords: FeV_2O_4 ; FeCr_2O_4 ; oxidation; nonisothermal kinetics; mechanism

1. Introduction

Crystalline materials with spinel structure and general chemical formula AB_2X_4 (A and B are usually metal cations) have been widely studied for their magnetic and dielectric properties [1–3] and remarkable material applications. For example, the well-known ferrovandium spinel (FeV_2O_4) and ferrochrome spinel (FeCr_2O_4) compounds with unique crystal structures exhibit normal cubic spinel structures at room temperature (space group $Fd\bar{3}m$) [4–6].

Spinel structure materials have recently attracted widespread technological attention owing to their exceptional electromagnetic properties [7–10]. Spinel FeV_2O_4 exhibits large capacity and high abundance, making it a crucial anode material for lithium-ion batteries and electronic devices [11–13], has potential as a photoelectric material and catalyst with broad application prospects [14–16], and in combination with other compounds, demonstrates boosted antibacterial properties [17–18]. Spinel FeCr_2O_4 has wide applications in photocatalysis [19], pollutant degradation [20], and gas sensing [8] owing to its excellent electrocatalytic activity

and stability. Although both spinels show superiority in several applications, their efficacy may be compromised by oxidation at high temperatures and complex environmental conditions [21–24].

Spinel FeV_2O_4 and spinel FeCr_2O_4 are also the predominant phases in high-chromium vanadium slag [25]. However, owing to the similar physical and chemical properties of vanadium and chromium, extracting these oxides from high-chromium vanadium slag presents significant challenges [26–27]. The primary method for vanadium extraction is sodium roasting–water leaching vanadium extraction; however, during roasting, competition between sodium vanadate and sodium chromate formed by oxidation and combination with sodium salts, respectively, results in significant competition between them. The selective separation of vanadium and chromium by roasting–leaching challenges achieving clean usage of such slag. Thus, elucidating the oxidation evolution law of ferrovandium and ferrochrome spinels during oxidation roasting is essential for improving the vanadium recovery rate.

This study presents the successful preparation of high

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crystallinity pure FeV_2O_4 and FeCr_2O_4 by high-temperature solid-state reaction. Their oxidation behavior in air is extensively examined for the first time by thermogravimetry (TG) and *in-situ* X-ray diffraction (XRD). The focus of this study was to understand both compounds' oxidation reactions at high temperatures as well as phase transitions at different temperatures and determine the final products. This study provides a theoretical basis for the applications of spinel materials in batteries, catalysts, and oxidation roasting–leaching processes of vanadium chromium slag.

2. Experimental

2.1. Materials preparation

FeV_2O_4 was synthesized by high-temperature solid-state reaction. Briefly, V_2O_5 (>99.9% purity, Shanghai Mackin Biochemical Co. Ltd., China) and Fe_2O_3 (99.99% purity, Aladdin Chemical Reagent Co. Ltd., China) were stoichiometrically weighed and thoroughly mixed before being finely ground into powder using an agate mortar by adding ethanol as required. Then, the mixture was loaded into a molybdenum crucible and placed in a tube furnace (GSL-1700X-VT, Hefei Kejing Group, China). The temperature was gradually increased from room temperature to 1200°C at 5 K/min and held at this temperature for 12 h. A gas mixture (volume ratio is $\text{CO}_2/\text{H}_2 = 0.7$) was continuously flown through the tube at 200 mL/min during the heating and cooling stages [28–29]. Finally, the product was cooled to ambient temperature within the furnace before being ground for subsequent characterization.

FeCr_2O_4 was prepared by the above method but with Fe_2O_3 (99.99% purity, Aladdin Chemical Reagent Co. Ltd., China) and Cr_2O_3 (>99.9% purity, Shanghai Mackin Biochemical Co. Ltd., China) as starting materials.

2.2. Thermogravimetric analysis

TG analyzer (Setaram Evo TG-DTG 1750, Setaram Instrumentation, France) was used for nonisothermal oxidation tests of FeV_2O_4 (FeCr_2O_4) powders. Approximately 20 mg of sample was loaded into an alumina crucible and then heated in a dynamic air atmosphere at 20 mL/min from room temperature to 700°C (900°C) at three heating rates (β) of 5, 10, and 15 K/min.

2.3. Thermodynamic analysis and characterization

Thermodynamic analysis was conducted with FactSage 8.1, in which Gibbs-free energies of the chemical reactions were calculated using the reaction module. The FactPS and FToxid databases were applied.

The crystal structures of the synthesized FeV_2O_4 and FeCr_2O_4 , as well as their oxidation products, were characterized using an XRD (Aeries, Malvern Panalytical, Netherlands) with $\text{Cu K}\alpha$ radiation at 40 kV and 8 mA. An *in-situ* XRD with $\text{Cu K}\alpha$ radiation (Empyrean, PANalytical B.V., Holland) equipped with platinum heating components and a corundum crucible was used in the experiments to determine

the phase composition during the solid reaction process at high temperatures for a better understanding of the reaction process. Phase analysis and Rietveld refinement were performed using High-score Plus 5.0 software with the international centre for diffraction data (ICDD) database.

3. Results and discussion

3.1. Characterization of FeV_2O_4 and FeCr_2O_4

Fig. 1 presents the XRD patterns and Rietveld graphs of the synthesized FeV_2O_4 and FeCr_2O_4 . The XRD pattern and Rietveld graph of the synthesized FeV_2O_4 in Fig. 1(a) show excellent agreement with the standard JCPDS (No. 96-901-2330) pattern of coulsonite (FeV_2O_4) of cubic phase with space group $Fd\bar{3}m$, demonstrating a high level of conformity. Refinement with R -weighted pattern (R_{wp}) obtained an impressively low R_{wp} value (2.53%), showing a highly reliable refinement procedure. The refined unit cell parameters for the crystal structure were $a = b = c = 8.4562 \text{ \AA}$, closely matching those reported in JCPDS No. 96-901-2330 ($a = b = c = 8.4530 \text{ \AA}$). The XRD pattern and Rietveld graph of the synthesized FeCr_2O_4 in Fig. 1(b) show good agreement with the standard JCPDS (No. 00-034-0140) pattern of coulsonite (FeCr_2O_4) belonging to the cubic phase with space group $Fd\bar{3}m$, further confirming its accuracy with a low R_{wp} value (3.56%). The refined unit cell parameters for the crystal structure were $a = b = c = 8.3780 \text{ \AA}$, closely resembling those in JCPDS No. 00-034-0140 ($a = b = c = 8.3790 \text{ \AA}$).

3.2. TG-DTG analysis

Fig. 2 presents the TG curves of FeV_2O_4 and FeCr_2O_4 at different heating rates in air. The FeV_2O_4 exhibits a slow rate of oxidation below 400°C with a minimal weight increase of less than 1.00wt%. Exceeding 450°C, the oxidation rate gradually increases with a progressive weight gain from 1.00wt% to almost 3.00wt% with increasing temperature from 450 to 530°C. The compound exhibits an accelerated oxidation rate and increased weight gain of up to 12.00wt% at around 575°C. Upon reaching temperatures nearing 650°C, FeV_2O_4 undergoes almost complete oxidation with a relatively stable weight gain. For the FeCr_2O_4 sample, in Fig. 2(b), it gradually oxidizes at 280°C, with a sharp increase in the oxidation rate beyond 420°C. The weight gain caused by oxidation dramatically increases from approximately 0.50wt% at 400°C to about an average value of 2.50wt% within the range of 480–520°C. Further increasing to 900°C slows down the oxidation rate, while the weight gain progressively increases to approximately 3.50wt%. These results show that FeV_2O_4 and FeCr_2O_4 at different heating rates exhibit similar final weight gains, which are close to theoretical values of approximately 18.00wt% and 3.57wt%, respectively.

Fig. 3 presents the differential thermogravimetry (DTG) curves of FeV_2O_4 and FeCr_2O_4 . The peak temperature of the DTG curves almost shifts toward a high temperature from 5 to 15 K/min, which can be attributed to heat transfer issues

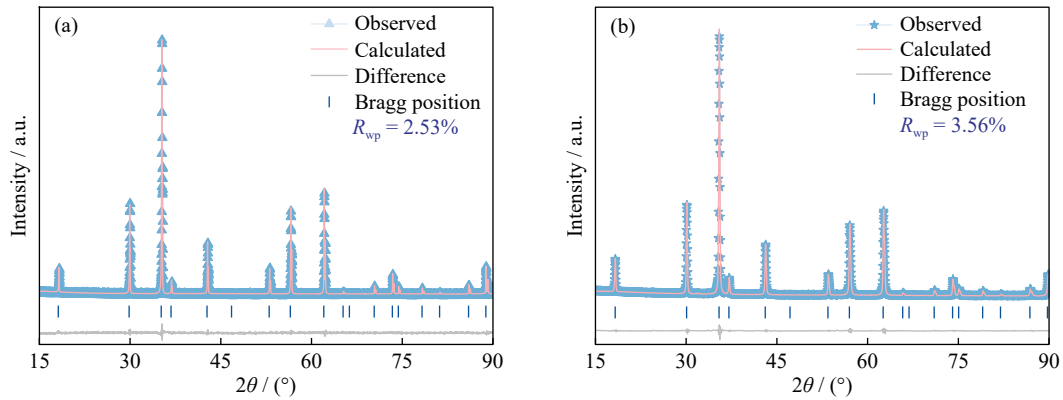


Fig. 1. XRD and Rietveld graphs of the synthesized (a) FeV₂O₄ and (b) FeCr₂O₄.

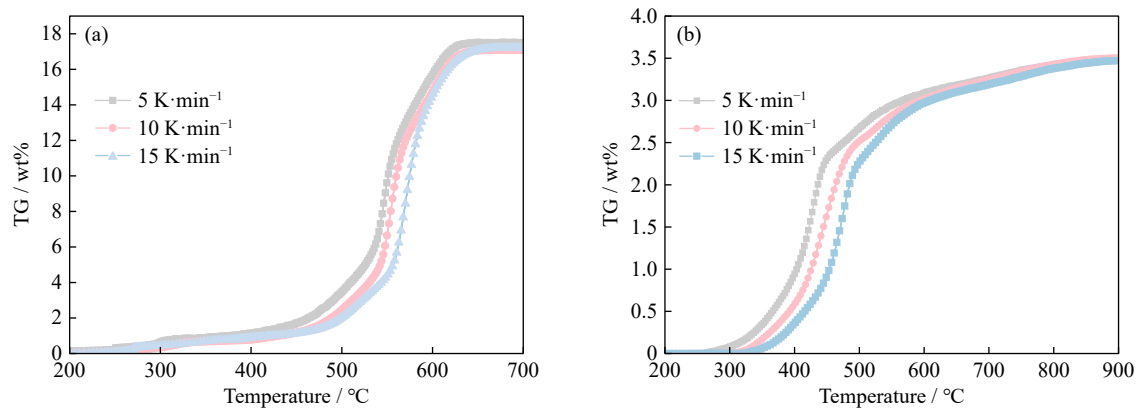


Fig. 2. TG curves of (a) FeV₂O₄ and (b) FeCr₂O₄ at different heating rates.

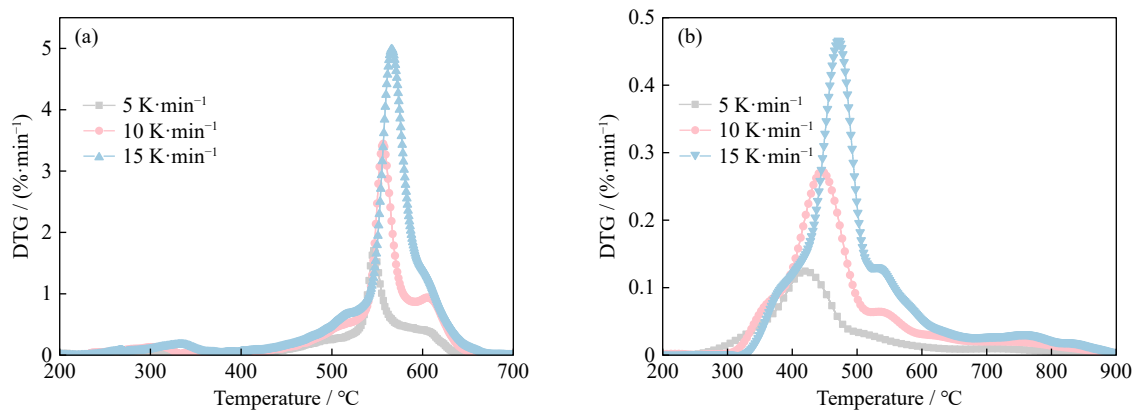


Fig. 3. DTG curves of (a) FeV₂O₄ and (b) FeCr₂O₄ at different heating rates.

between the sample and instrument. In Fig. 3, both samples display four distinct peaks, representing the four stages of their oxidation. For the FeV₂O₄ sample, in the initial stage, a stable minor peak is observed below 463°C. In the second stage, a small platform appears at 463–543°C, with a sample weight gain of 2.72wt%–3.78wt%. In the third stage, an evident DTG peak is observed at 531–594°C, with a sample weight gain of 8.07wt%–9.94wt%. In the final stage, a peak is observed at 575–668°C, with a sample weight gain of 3.30wt%–3.98wt%. Similarly, for FeCr₂O₄, the initial stage is represented by a small inflection point at 344–423°C, with a sample weight gain of 0.38wt%–0.53wt%. The second stage emerges at 363–525°C, with a sample weight gain of 1.92wt%–2.23wt%. In the third stage, a peak is observed at

495–633°C, with a sample weight gain of 0.45wt%–0.78wt%. In the final stage, a peak occurs at 600–876°C, with a sample weight gain of 0.37wt%–0.45wt%.

3.3. Oxidation degree analysis

Thermal kinetics analysis can measure the process of a chemical reaction (or phase transition). Among these, non-isothermal thermal analysis is the most widely used at multiple heating rates. In nonisothermal kinetic experiments, sample mass is related to temperature change, and the rule for changes in conversion rate under a specific heating rate is [30]:

$$\frac{d\alpha}{dt} = k(T)f(\alpha) \quad (1)$$

For dynamic data obtained at a specific heating rate $\beta = dT/dt$, $k(T)$ refers to the reaction rate constant and follows the Arrhenius equation $k(T) = A \exp[-E_a/(RT)]$. Then, Eq. (1) becomes:

$$\beta \frac{d\alpha}{dT} = A \exp\left(\frac{-E_a}{RT}\right) f(\alpha) \quad (2)$$

where E_a represents the apparent activation energy (kJ/mol), A represents the Arrhenius pre-exponential factor (s^{-1}), β represents the heating rate (K/min), R represents the universal gas constant ($8.314 \text{ J} \cdot \text{mol}^{-1} \cdot \text{K}^{-1}$), T represents the absolute temperature (K), t represents the time (s), and α is the degree of conversion and measures the extent of completion of a reaction as follows:

$$\alpha = \frac{m_0 - m_t}{m_0 - m_f} \quad (3)$$

where m_0 refers to the initial mass of the sample (mg), m_t refers to the mass of the sample at time t (mg), and m_f refers to the final mass of the sample after the reaction (mg).

Fig. 4 presents the α versus T curves at different heating rates for the oxidation reactions of FeV_2O_4 and FeCr_2O_4 . The conversion degrees of FeV_2O_4 and FeCr_2O_4 exhibit similar trends at different heating rates, i.e., an initial gradual in-

crease, then a rapid ascent, and finally a stable plateau. Increasing the heating rate from 5 to 15 K/min results in a shift in the conversion rate toward higher temperatures. The conversion rate of FeV_2O_4 is relatively slow below 450°C , while that of FeCr_2O_4 is slower below 350°C . In $500\text{--}600^\circ\text{C}$ for FeV_2O_4 and $400\text{--}600^\circ\text{C}$ for FeCr_2O_4 , the oxidation rates are significantly accelerated with show sharp increases in conversion degree. The complete oxidation of FeV_2O_4 occurs approximately at $600\text{--}700^\circ\text{C}$, as shown in Fig. 4(a). However, a gradual growth trend is still observed for FeCr_2O_4 at $650\text{--}900^\circ\text{C}$, as shown in Fig. 4(b), with complete oxidation occurring near 900°C .

Fig. 5 shows the first derivatives of the conversion degree of FeV_2O_4 and FeCr_2O_4 versus time. The oxidation rates of both compounds exhibit significant variations throughout the entire reaction process. The curve of FeV_2O_4 shows four stages of oxidation: stage I ($0.10 < \alpha < 0.22\text{--}0.26$), stage II ($0.22\text{--}0.26 < \alpha < 0.45\text{--}0.48$), stage III ($0.45\text{--}0.48 < \alpha < 0.70\text{--}0.80$), and stage IV ($0.70\text{--}0.80 < \alpha < 1.00$). Similarly, the oxidation process of FeCr_2O_4 also shows four stages: stage I ($0.10 < \alpha < 0.13\text{--}0.17$), stage II ($0.13\text{--}0.17 < \alpha < 0.43\text{--}0.45$), stage III ($0.43\text{--}0.45 < \alpha < 0.68\text{--}0.73$), and stage IV ($0.68\text{--}0.73 < \alpha < 1.00$).

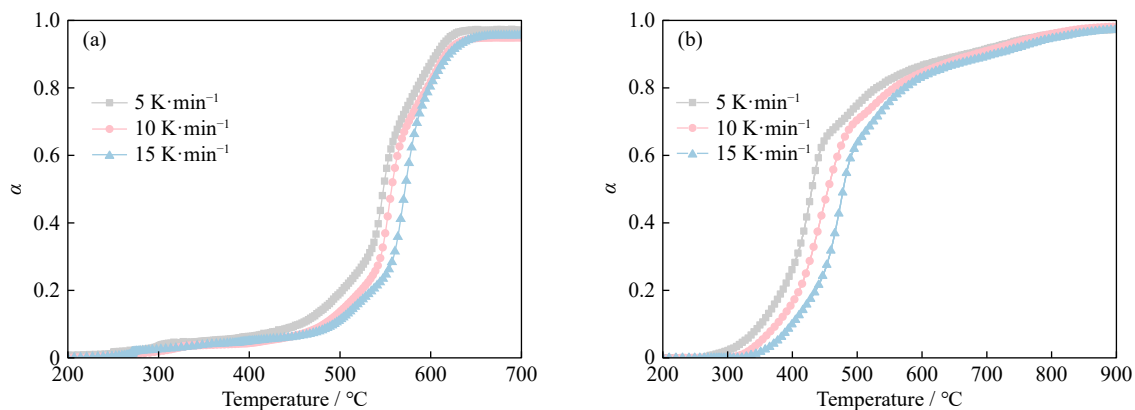


Fig. 4. α versus T curves for the oxidation of (a) FeV_2O_4 and (b) FeCr_2O_4 .

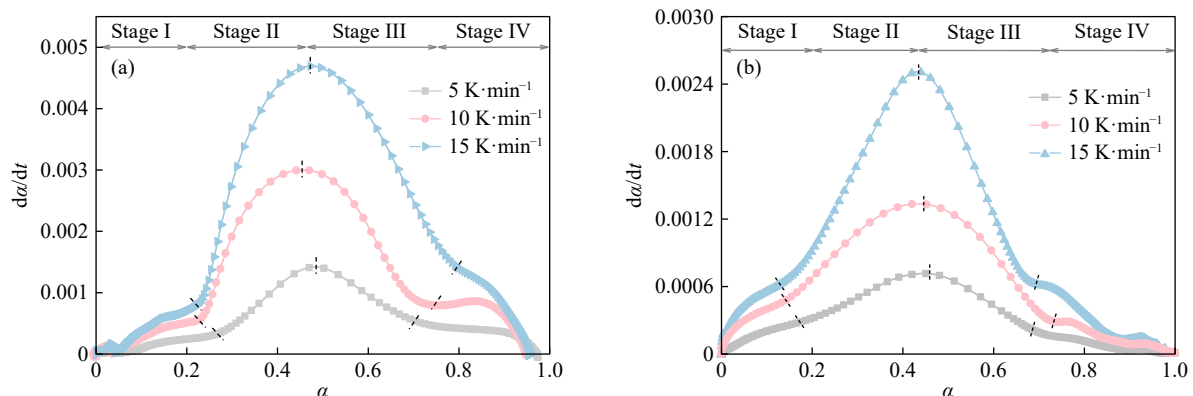


Fig. 5. First derivatives of conversion degree (α) versus time (t) at different heating rates for (a) FeV_2O_4 and (b) FeCr_2O_4 .

3.4. Reaction activation energy

The isoconversional method is widely used because it determines a relatively reliable activation energy value, neglecting the chemical reaction mode function. Herein, the Kis-

singer–Akahira–Sunose (KAS) method was used to determine the activation energies of FeV_2O_4 and FeCr_2O_4 by nonisothermal thermal analysis.

The KAS formula can be expressed as [31–32],

$$\ln\left(\frac{\beta}{T_\alpha^2}\right) = \ln\left(\frac{AR}{E_\alpha G(\alpha)}\right) - \frac{E_\alpha}{RT_\alpha} \quad (4)$$

where T_α represents the thermodynamic temperature corresponding to the specified α value, E_α represents the activation energy (kJ/mol) corresponding to the specified α value, and $G(\alpha)$ represents the integral form of the kinetic mode func-

tion. The T_α corresponding to the same α value is taken at different heating rates. Apparent activation energy can be obtained from the $\ln(\beta/T^2)$ versus $1/T$ plot for a given value of conversion degree (α), where the slope is equal to $-E_\alpha/R$. Fig. 6 presents the $\ln(\beta/T^2)$ against $1/T$ plots of FeV₂O₄ and FeCr₂O₄ for α of 0.10–0.90 with a step of 0.05.

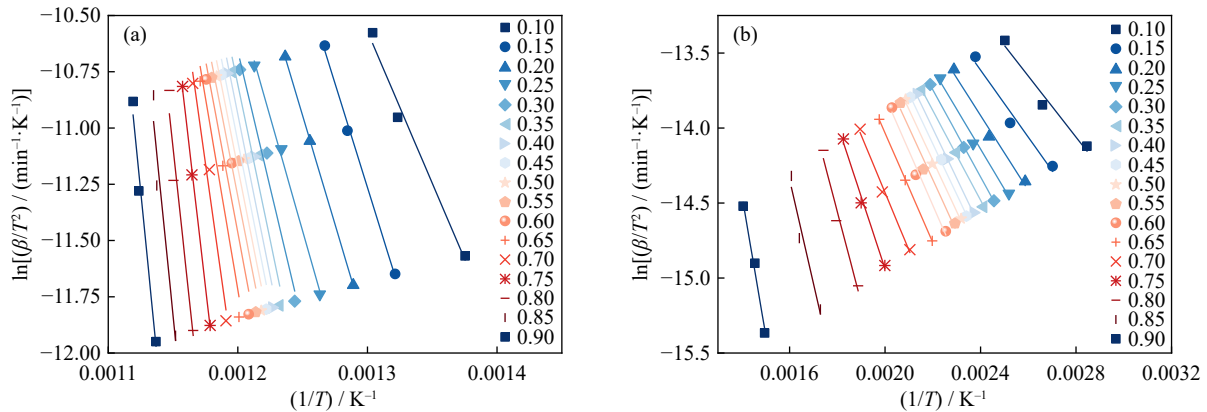


Fig. 6. Determination of activation energy by the KAS method: (a) FeV₂O₄; (b) FeCr₂O₄.

Fig. 7 shows the variation in the activation energy of the oxidation of FeV₂O₄ and FeCr₂O₄ with conversion degree by the KAS method. The apparent activation energy for the oxidation of FeV₂O₄ is much higher and more varied than that of FeCr₂O₄, indicating greater complexity in the oxidation mechanism of FeV₂O₄ than FeCr₂O₄. This suggests that a higher activation energy is required for the transition of reactant molecules from the ground state to the activated state in FeV₂O₄. This also indicates that the reaction pathway of FeCr₂O₄ may be simpler and more direct than FeV₂O₄, without significant energy barriers or obstacles. In addition, the higher apparent activation energy of FeV₂O₄ implies the great influence of temperature on the oxidation of FeV₂O₄, while FeCr₂O₄ displays higher thermal stability, as depicted by its higher maximum oxidation temperature than that of FeV₂O₄.

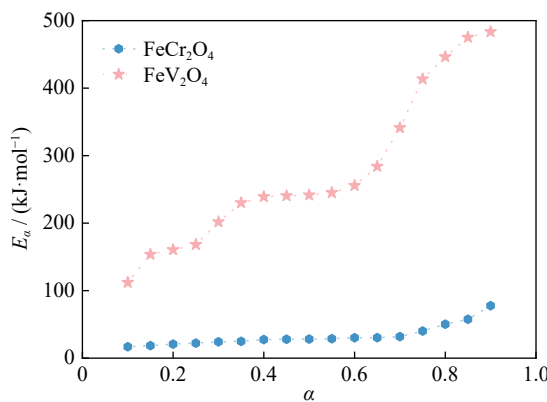


Fig. 7. Activation energy versus conversion degree plots of FeV₂O₄ and FeCr₂O₄ oxidation.

The apparent activation energy of FeV₂O₄ oxidation displays significant variations, which can be roughly divided into four stages based on the previous analysis. In the first

stage, the activation energy gradually increases from 112.00 to 160.50 kJ/mol with the progression of the oxidation reaction. In the second stage, a slight elevation in activation energy is observed between 160.50 and 240.80 kJ/mol during ongoing oxidation reactions. In the third stage, a rapid escalation in activation energy occurs, elevating it from 240.80 to 413.40 kJ/mol alongside the oxidation reaction process. In the fourth stage, an ultimate increase in activation energy up to 483.40 kJ/mol is observed due to continued oxidation. For FeCr₂O₄, its apparent activation energy shows a slight increase from 16.90 to 32.00 kJ/mol below a conversion degree of about 0.70. Further increasing the conversion degree from about 0.70 to 0.90 results in a significant increase in apparent activation energy to 77.60 kJ/mol, demonstrating the increase in difficulty in the later stages of the oxidation process compared with the earlier stages. It can also be observed that during the linear heating process, the conversion degree of FeCr₂O₄ can quickly increase from 0 to about 0.7 at 300–500°C, while it only gradually increases from about 0.70 to approximately 1.00 at 500–900°C, as shown in Fig. 4(b). The nonlinear changes of different conversion degrees and apparent activation energies of FeV₂O₄ and FeCr₂O₄ imply an inconsistent reaction mechanism throughout the oxidation process, indicating the presence of multiple competitive reactions, as further supported by the DTG results.

3.5. Reaction model analysis

The Malek method is a kinetic analysis method based on the multihating rate method that can be used to determine the reaction mechanism and is widely accepted for its simplicity and accuracy [33–34].

According to the reaction rate Eq. (5) and the Coats–Redfern Eq. (6) [35],

$$\frac{d\alpha}{dt} = A \exp\left(-\frac{E}{RT}\right) f(\alpha) \quad (5)$$

$$G(\alpha) = \int_0^\alpha \frac{d\alpha}{f(\alpha)} = \frac{ART_\alpha^2}{E\beta} \exp\left(-\frac{E}{RT_\alpha}\right) \quad (6)$$

It can be concluded that:

$$G(\alpha) = \frac{RT_\alpha^2}{E\beta} \frac{d\alpha}{dt} \frac{1}{f(\alpha)} \quad (7)$$

When $\alpha = 0.5$,

$$G(0.5) = \frac{RT_{0.5}^2}{E\beta} \left(\frac{d\alpha}{dt}\right)_{0.5} \frac{1}{f(0.5)} \quad (8)$$

where $(d\alpha/dt)_{0.5}$ represents the reaction rate during the whole reaction process when $\alpha = 0.5$. $Y(\alpha)$ and $y(\alpha)$ are defined by the ratio of Eqs. (7)–(8). Consequently, Eqs. (9)–(10) can be obtained as

$$Y(\alpha) = \left(\frac{T}{T_{0.5}}\right)^2 \frac{\left(\frac{d\alpha}{dt}\right)}{\left(\frac{d\alpha}{dt}\right)_{0.5}} = \frac{f(\alpha) \cdot G(\alpha)}{f(0.5) \cdot G(0.5)} \quad (9)$$

and

$$y(\alpha) = \left(\frac{T_i}{T_{0.5}}\right)^2 \frac{\left(\frac{d\alpha}{dt}\right)_i}{\left(\frac{d\alpha}{dt}\right)_{0.5}} \quad (10)$$

where T_i and $(d\alpha/dt)_i$ represent the temperature and reaction rate at the point α_i , respectively.

In this study, the most probable $f(\alpha)$ is determined based

on the standard curve $y(\alpha)$ – α . The relationship between actual $y(\alpha)$ and α can be obtained by experimental data with three heating rates. If the experimental data curve coincides with or if all the experimental data points fall on a standard curve, then $f(\alpha)$ or $G(\alpha)$ corresponding to that standard curve is determined as the most likely kinetic mechanism function. Fig. 8 illustrates the relationship between the standard curve $y(\alpha)$ and the experimental curve $y(\alpha)$ of FeV_2O_4 and FeCr_2O_4 oxidation.

For FeV_2O_4 , in the conversion degree of 0.10–0.26, the three experimental curves agree well with the No. 35 standard curve. The function corresponding to curve 35 is the reaction series equation, the mechanism is $n = 4$, and the differential form of the mechanism function $f(\alpha) = \frac{1}{4}(1-\alpha)^{-3}$ is the integral $G(\alpha) = 1 - (1-\alpha)^4$. No satisfactory correlation with any curve is observed in the second and third stage ranges, suggesting the presence of multiple oxidation mechanisms for FeV_2O_4 at this stage, resulting in poor agreement with experimental data, requiring further analysis to elucidate the specific mechanism function. During the progression of the reaction, as the experimental curve ranges from 0.68 to 0.95, the $\beta = 5$ K/min curve gradually approaches the standard curves of 39 and 40 (following an exponential law). The curves obtained at $\beta = 10$ and 15 K/min closely resemble the standard curves of 36, 38, and 41, which correspond to chemical reactions.

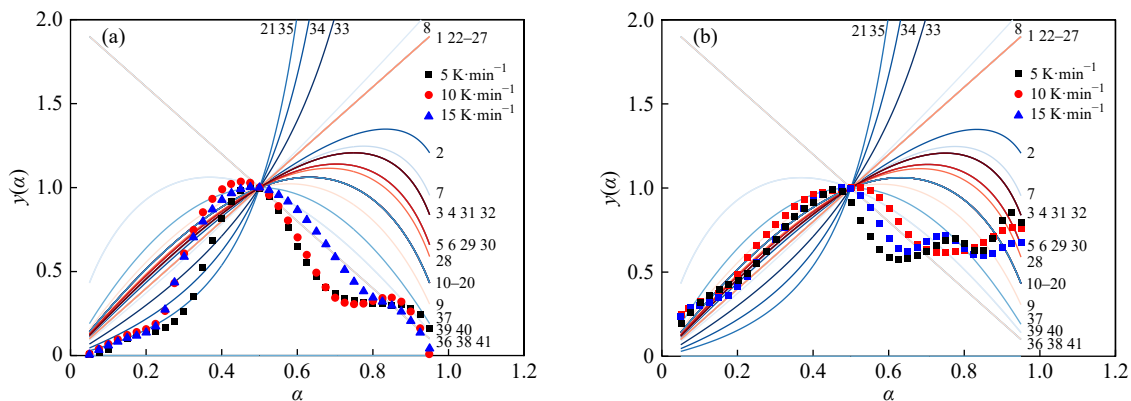


Fig. 8. Experimental data points and standard curves of (a) FeV_2O_4 and (b) FeCr_2O_4 by the Malek method.

For FeCr_2O_4 , the three experimental curves display characteristics of the three-position diffusion model in the first and second stages, but the involved specific mechanism function requires further analysis. Notably, the experimental curve in conversion degree 0.43–0.95 is similar to that of FeV_2O_4 , demonstrating multiple mechanism functions. Combined with the KAS results, this stage represents the gradual transition process from a three-dimensional diffusion model to a chemical reaction.

3.6. In-situ XRD analysis

In-situ XRD was performed to describe the oxidation process of FeV_2O_4 and FeCr_2O_4 , as shown in Fig. 9. The diffraction peak intensity of FeV_2O_4 gradually decreases, while

those of Fe_3O_4 , V_2O_3 , and Fe_2O_3 gradually increase at 200–450°C, as shown in Fig. 9(a). At 500–650°C, most of the intermediates are oxidized, which results in the identification of the diffraction peaks corresponding to VO_2 , V_6O_{13} , and FeV_2O_4 . The oxidation state of vanadium gradually shifts from V^{3+} and V^{4+} to V^{5+} , forming vanadium pentoxide, which has a relatively low melting point of 943 K (670°C). Because vanadium pentoxide volatilization or continuous production of vanadium pentoxide may exist in liquid and amorphous states [36–37], where there is not much volatilization and more of it is in the melting state, the intensity of the diffraction peak is significantly reduced. However, in the oxidation process, the oxidized Fe/V ratio changes and the volatilization of vanadium pentoxide is about 0.2% [38–39], resulting

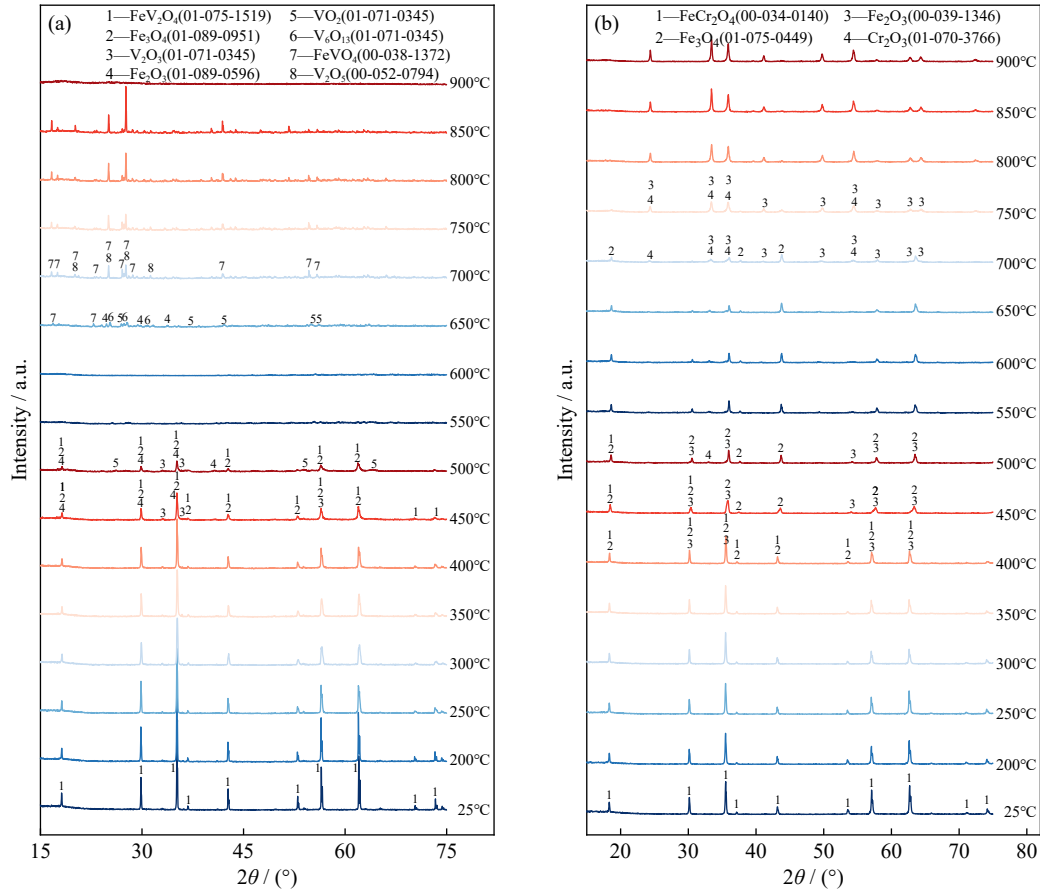


Fig. 9. *In-situ* XRD patterns of (a) FeV₂O₄ and (b) FeCr₂O₄ at different temperatures.

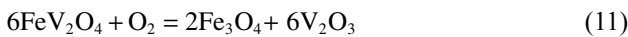
in a reduction in vanadium in the sample but relatively small compared with the total sample. Above 700°C, the diffraction peaks corresponding to FeV₂O₄ vanish, while those of FeVO₄ and V₂O₅ as final products tend to stabilize.

In Fig. 9(b), the oxidation process of FeCr₂O₄ is similar to that of FeV₂O₄. At 200–400°C, the diffraction peak intensity of FeCr₂O₄ gradually decreases. At 450–700°C, the diffraction peak changes and new substances are produced. Finally, above 750°C, the diffraction peak intensities of Fe₂O₃ and Cr₂O₃ gradually increase and become stable, demonstrating complete oxidation reaction.

3.7. Derivation of the oxidation mechanism

3.7.1. Derivation of the FeV₂O₄ oxidation mechanism

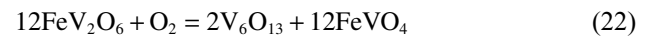
The oxidation process of FeV₂O₄ is highly intricate, involving numerous intermediates. Based on the *in-situ* XRD and TG-DTG results, the oxidation pathway of FeV₂O₄ is outlined as follows. In the initial oxidation stage of FeV₂O₄ (200–450°C), the reaction is



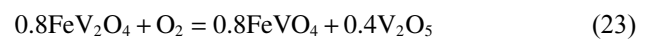
As the temperature continues to increase, the oxidation reactions that may occur in the middle oxidation stage (450–700°C) are



Previous work [40] has confirmed the presence of solid solution FeV₂O₆ formed by oxidation of FeV₂O₄ at 470–580°C, which is formed through oxidation of FeV₂O₄. However, no FeV₂O₆ phase was detected in this study from the *in-situ* XRD results, suggesting the possibility of a subsequent rapid oxidation reaction occurring for FeV₂O₆ as an intermediate.



Adding the three formulas, the total reaction equation is



The oxidation mechanism of FeV₂O₄ was further confirmed by calculations of the Gibbs-free energies of the chemical reactions at each stage. In Fig. 10, all reactions exhibit $-\Delta G$ values across the entire temperature range considered, indicating their possibility. Reactions (18) and (12) involving Fe₃O₄ have the lowest ΔG values at temperatures

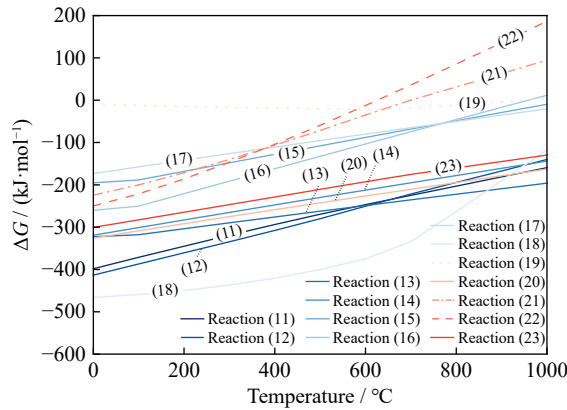


Fig. 10. Gibbs-free energy changes for possible reactions during the FeV_2O_4 oxidation.

below 850 and 600°C, respectively, suggesting their greater propensity toward oxidation reactions. The intermediate V_2O_3 undergoes easy oxidation to generate VO_2 , which is

further oxidized to V_6O_{13} and V_2O_5 . Reactions (21) and (22) can only spontaneously react below 640 and 590°C, respectively. As the reaction progresses, Fe_2O_3 and V_2O_5 eventually react to form FeVO_4 (reaction (19)).

From the above analysis, the oxidation pathway of FeV_2O_4 oxidation in air can be derived and is illustrated in Fig. 11.

3.7.2. Derivation of the FeCr_2O_4 oxidation mechanism

The oxidation process of FeCr_2O_4 is relatively straightforward. Based on the *in-situ* XRD and TG-DTG results, FeCr_2O_4 does not oxidize during the initial stage (200–400°C). However, significant changes in the XRD pattern are observed during the middle oxidation stage (450–700°C), indicating the potential occurrence of oxidation reactions.

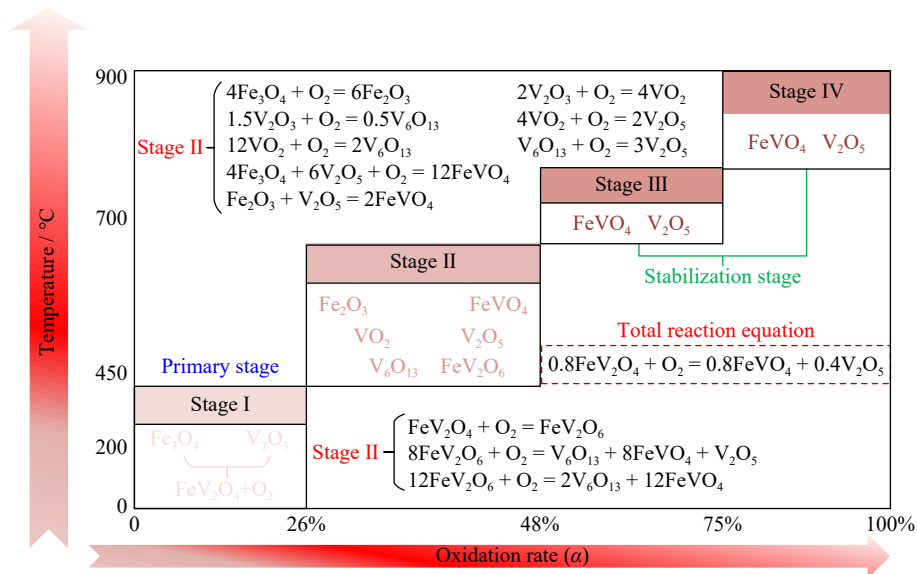
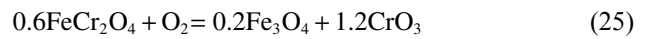
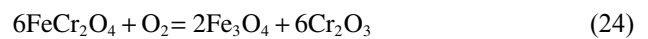


Fig. 11. Schematic of the oxidation pathway of FeV_2O_4 .

The Gibbs-free energy of reaction (25) is observed to be greater than 0 in 0–1000°C, as depicted in Fig. 12, suggesting that under the experimental conditions, chromium did not undergo oxidation to the hexavalent state.

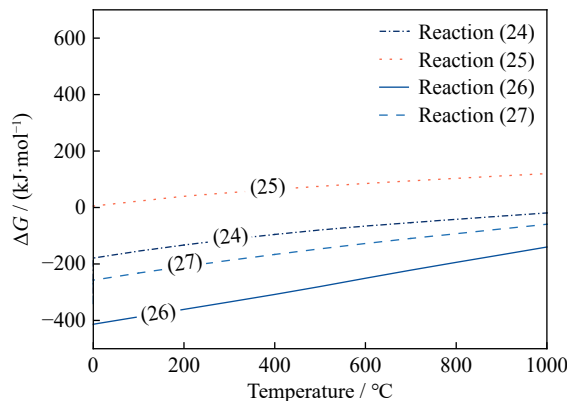
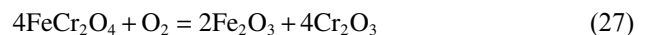


Fig. 12. Gibbs-free energy changes for possible reactions during the FeCr_2O_4 oxidation process.

With increasing temperature, Fe_3O_4 can also react with air to form Fe_2O_3 .



The oxidation of FeCr_2O_4 basically stops above 700°C, yielding Fe_2O_3 and Cr_2O_3 as the final products. Thus, the total reaction is



The Gibbs-free energies of reactions (24), (26), and (27) in air from 0 to 1000°C are shown in Fig. 12. These reactions exhibit $-\Delta G_r$ values within this temperature range, indicating their possibility. Notably, the ΔG_r value of reaction (25) is more negative than that of reaction (24), suggesting the oxidation of Fe_3O_4 from reaction (24) to Fe_2O_3 .

Based on the above analysis, the oxidation pathway of FeCr_2O_4 in air can be derived and is illustrated in Fig. 13.

Based on the above comprehensive analysis, both the oxidation mechanisms of spinel FeV_2O_4 and spinel FeCr_2O_4 are

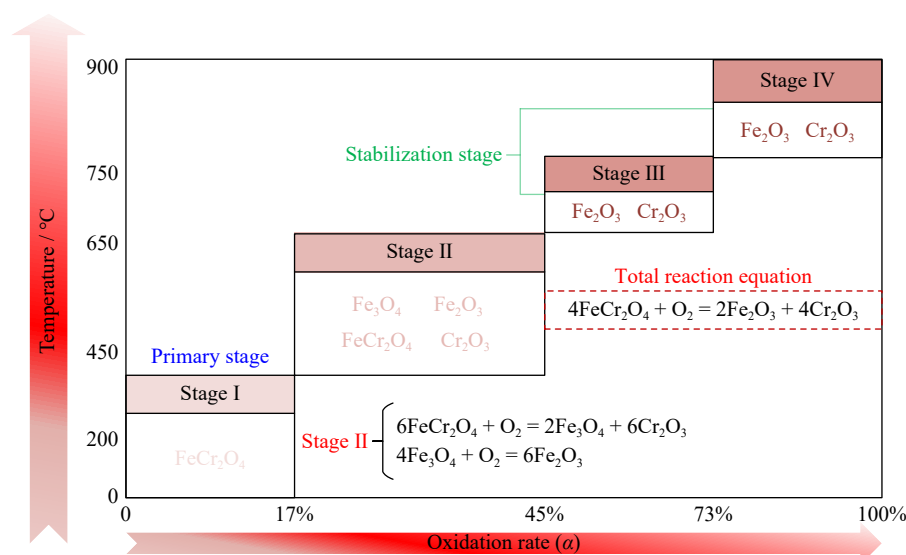


Fig. 13. Schematic of the oxidation pathway of FeCr₂O₄.

highly intricate. Furthermore, thoroughly exploring their oxidation behavior has significant implications for practical applications. For instance, during the roasting process of vanadium and chromium slag, spinel FeV₂O₄ and spinel FeCr₂O₄ serve as the main phases of the slag. By controlling the degree of oxidation for these spinel phases, optimization of the leaching and extraction processes for vanadium and chromium can be performed for improvement in recovery rates and reduction in production costs. In fact, researchers have utilized the differences in oxidation, conversion, and thermodynamics between ferrovanadium spinel and ferrochrome spinel in the roasting process to extract vanadium and chromium by different techniques such as two-stage roasting, fractional roasting, and selective extraction of vanadium [27,41–43]. These methods also emphasize the importance of fully understanding the oxidation mechanism of ferrovanadium and ferrochrome spinels. This work provides technical support for efficient, green, and low-carbon recovery of vanadium and chromium from vanadium chromium slag, thus improving resource utilization capabilities.

4. Conclusions

The following conclusions can be drawn:

(1) The oxidation process of FeV₂O₄ and FeCr₂O₄ can be divided into four stages. The third stage has the significant contribution to the weight gain of FeV₂O₄, with an increase of 8.07wt%–9.94wt%. The second stage predominantly contributes to the weight gain of FeCr₂O₄, ranging from 1.92wt% to 2.23wt%.

(2) The oxidation of FeV₂O₄ has a much higher apparent activation energy than that of FeCr₂O₄. Their oxidation mechanisms are complex and have distinct mechanism functions. In particular, the chemical reaction controls the entire oxidation process for FeV₂O₄, whereas that for FeCr₂O₄ transitions from a three-dimensional diffusion model to a chemical reaction model.

(3) *In-situ* XRD results reveal numerous intermediate

products during the oxidation process of both compounds, finally forming the final products FeVO₄ and V₂O₅ for FeV₂O₄ and Fe₂O₃ and Cr₂O₃ for FeCr₂O₄, respectively.

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Conflict of Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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