

## Thermoelectric properties of quaternary $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$ alloys

Hao Yin, Xin-Bing Zhao, Qian Zhang, and Tie-Jun Zhu

State Key Laboratory of Silicon Materials, Department of Materials Science and Engineering, Zhejiang University, Hangzhou 310027, China  
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**Abstract:** Quaternary alloys  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$  ( $x=0, 0.02, 0.05, 0.08, 0.1, \text{ and } 0.2$ ) were prepared using induction melting followed by hot-pressing. Relative densities of the sintered samples were over 97% of the theoretical values. Multiple phases were detected in the samples. It was found that the Seebeck coefficient was sensitive to the content of  $\text{Mg}_2\text{Ge}$  and a maximum value of about  $350 \mu\text{V}\cdot\text{K}^{-1}$  was obtained. The introduction of Ge increases the electrical conductivity and the thermal conductivity simultaneously. The mechanism of this phenomenon was discussed. A maximum dimensionless figure of merit,  $ZT$ , of about 0.28 was obtained for  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.55}\text{Ge}_{0.05}$  at 550 K.

**Key words:** thermoelectric materials; hot-pressing; thermal conductivity; induction melting; quaternary alloys

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### 1. Introduction

Both energy shortage and environmental burden compel us to seek for all kinds of new resources. New power generators are all characterized by clean, green, or renewable. Among these, thermoelectric (TE) power generators, which can directly convert heat into electricity, are gaining more and more focuses recently because of their unique advantages such as no moving parts, no noise, less maintenance, and long life [1-4]. Dimensionless figure of merit  $ZT = \alpha^2 \sigma T / \kappa$  of TE materials is usually used to evaluate the efficiency of a TE device, where  $\alpha$  is the Seebeck coefficient,  $\sigma$  the electrical conductivity,  $\kappa$  the thermal conductivity, and  $T$  the Kelvin temperature.  $\alpha^2 \sigma$  is also defined as the power factor to determine the electrical property of TE materials. The constituent elements of  $\text{Mg}_2\text{-IV}$  (IV is Si, Sn, or Ge) compound, as a kind of TE materials, are environmental friendly and cheap. Thus,  $\text{Mg}_2\text{Si}$ ,  $\text{Mg}_2\text{Sn}$ , and  $\text{Mg}_2\text{Ge}$  are expected to be promising TE materials for power generation in the middle temperature range (400-800 K) [5-9]. In this paper, quaternary alloys  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$  were prepared by induction melting and hot-pressing to increase electrical conductivity and optimize the semiconductor properties, which has not been reported be-

fore.

### 2. Experimental

The starting materials of  $\text{Mg}_2\text{Si}$ ,  $\text{Mg}_2\text{Sn}$ , and  $\text{Mg}_2\text{Ge}$  were prepared by induction melting of constituent elements of granular Mg (99.9% in purity), Si (99.9999%), Sn (99.9%), and Ge (99.999%). The ingots gained were ground into powder (under  $40 \times 10^{-6}$  m in diameter). The powders were mixed to the designed compositions of  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$  ( $x=0, 0.02, 0.05, 0.08, 0.1, 0.2$ ), and hot-pressed under a pressure of 80 MPa at 973 K for 2 h in vacuum. The disks obtained were 12.6 mm in diameter with a thickness of about 2 mm. Relative densities of the compacts measured by the Archimedes method were about 97% of the theoretical values. X-ray powder diffraction (XRD) was conducted on a RigakuD/MAX-2550PC diffractometer using Cu  $K_\alpha$  radiation ( $\lambda=1.5406 \times 10^{-10}$  m). The samples of necessary size for electrical and thermal measurements were cut from the disks. The Seebeck coefficient  $\alpha$  and electrical conductivity  $\sigma$  were measured from room temperature to 723 K using a four-probe method. The temperature difference between both ends of the sample for measuring the Seebeck coefficient was about 5 K. Electrical conductivity was calculated from the sample dimensions and the

average resistance measured with the forward and reversed currents [10]. The thermal diffusivity  $D$  and the specific heat capacity  $C_p$  of the samples were measured by a laser flash apparatus (Netzsch LFA 457) and a thermal analyzer (Netzsch DSC 404), respectively. The thermal conductivity was then calculated from the relationship  $\kappa = \rho DC_p$ , where  $\rho$  is the density of the material.

### 3. Results and discussion

XRD patterns of  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$ , ( $x = 0, 0.02, 0.05, 0.08, 0.1, 0.2$ ) are shown in Fig. 1. All the peaks of the samples can be indexed to  $\text{Mg}_2\text{Si}$ ,  $\text{Mg}_2\text{Sn}$ , and  $\text{Mg}_2\text{Ge}$  based solid solution phases with the face-centered cubic structure and the space group of  $Fm\bar{3}m$ , indicating that the samples are composed of multiple phases. Furthermore, as Ge increases, the peaks indexed to the same diffraction crystal plane move closer, which means that Ge improves the solid solubility between both Si- and Sn-rich phases. This might be because Ge, whose atom radius ( $1.22 \times 10^{-10}$  m) is between Si ( $1.11 \times 10^{-10}$  m) and Sn ( $1.41 \times 10^{-10}$  m), decreases the lattice size difference between  $\text{Mg}_2\text{Si}$  and  $\text{Mg}_2\text{Sn}$  phases [11].

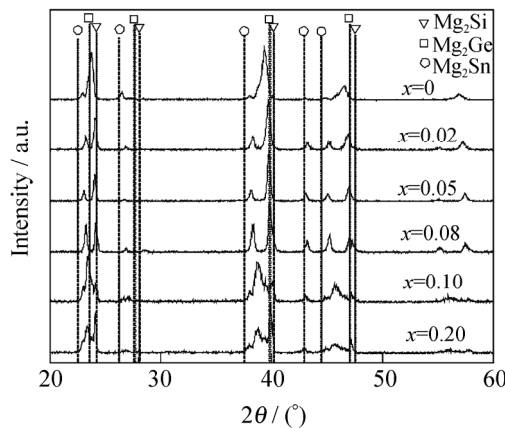


Fig. 1. XRD patterns of  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$ .

Absolute values of the Seebeck coefficient of all the samples are displayed in Fig. 2, plotted as a function of the measuring temperatures. The samples with  $x \leq 0.08$  are n-type while  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.4}\text{Ge}_{0.2}$  and  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.5}\text{Ge}_{0.1}$  show p-type characters. This phenomenon might be caused by the conductivity of  $\text{Mg}_2\text{Ge}$ , which is p-type, different from the n-type conduction of  $\text{Mg}_2\text{Si}$  and  $\text{Mg}_2\text{Sn}$ . The maximum value of p-type samples is about  $325 \mu\text{V}\cdot\text{K}^{-1}$  at 400 K for  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.4}\text{Ge}_{0.2}$ . The Seebeck coefficient of n-type compounds shows similar trends with the temperature and intensity dependence on composition. All the measured Seebeck coefficients ascend with temperature, reach peak values at about 550 K and go down at higher temperatures because of an increasing number of thermally excited minority carriers. A maximum

value of  $|\alpha| = 350 \mu\text{V}\cdot\text{K}^{-1}$  was obtained in  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6}$  ( $x=0$ ).

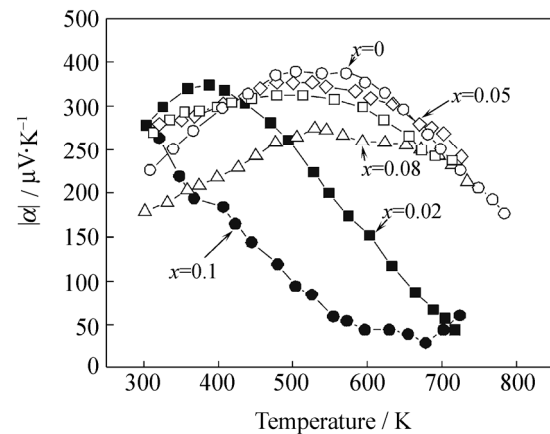
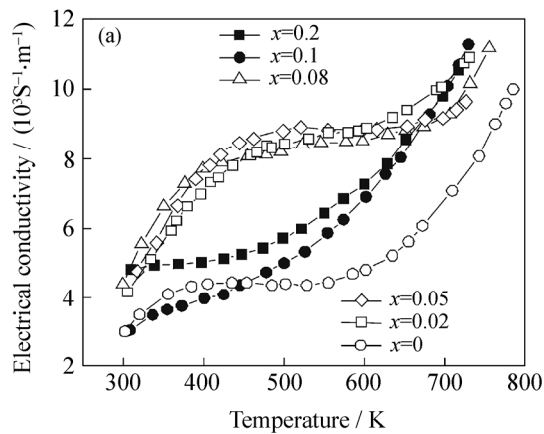


Fig. 2. Temperature dependence of  $|\alpha|$  for  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$  ( $\alpha$  of the samples with  $x=0, 0.02, 0.05$ , and  $0.08$  are negative).

Curves of electrical conductivity against temperature are plotted in Fig. 3(a). With the increase in Ge content, the electrical conductivities increase, reaching the maximum in sample  $x=0.05$ . All the electrical conductivities measured go up at lower temperatures, which are induced by increasing the carrier numbers. A mild platform can be observed which might be caused by the decrease of carrier mobility, and then a remarkable increase follows over 650 K which is believed to be affected by intrinsic excitations. Samples with  $x=0.02, 0.05, 0.08$  show higher values in the whole temperature range. The band gaps,  $E_g$ , are 0.77, 0.74, and 0.35 eV for  $\text{Mg}_2\text{Si}$ ,  $\text{Mg}_2\text{Ge}$ , and  $\text{Mg}_2\text{Sn}$ , respectively [11].  $E_g$  might decrease after adding  $\text{Mg}_2\text{Ge}$ , which makes it easier for electrons to jump from the valence band to conduction band. Thus, the electrical conductivity might increase. Fig. 3(b) is the relationship of  $\ln\sigma$  and  $1000/T$ . The calculated  $E_g$  values for all the samples with Ge are shown in Table 1 [12].

The temperature dependence of thermal conductivity  $\kappa$  of all the samples is shown in Fig. 4(a).  $\kappa$  consists of electronic contribution  $\kappa_{el}$  and lattice contribution  $\kappa_{ph}$ . According to the Wiedemann-Franz rule,  $\kappa_{el} = L_0 \sigma T$ , where  $L_0$  is the Lorenz number  $2.45 \times 10^{-8} \text{V}^2\cdot\text{K}^2$  for heavily doped semiconductors [13-14]. All the electronic thermal conductivities calculated in these samples are far smaller than total  $\kappa$ . That is to say, lattice thermal conductivity plays predominant role in total  $\kappa$  [15]. In the ternary system Mg-Si-Sn, the difference in volume of atoms between Si and Sn strengthens the phonons scattering of crystal defects which dramatically reduce the thermal conductivity compared with  $\text{Mg}_2\text{Si}$ . However, in the quaternary system, Ge, whose atom volume is in the middle of Si and Sn, abates this effect. The upward trends that all

the samples show with the increase of  $x$  could support the conclusion. When the temperature exceeds 650 K, intrinsic excitations increase the  $\kappa$  values. The lowest thermal conductivity is obtained from  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6}$ , which is about  $1.65 \text{ W}\cdot\text{m}^{-1}\cdot\text{K}^{-1}$ . The ratios of  $\sigma/\kappa$  are



also calculated and presented in Fig. 4(b), from which we can see that the ratios of the samples with  $0 < x < 0.2$  are higher than that of  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6}$  ( $x=0$ ). This indicates that the solubility of Ge is an effective way to increase the thermoelectric properties.

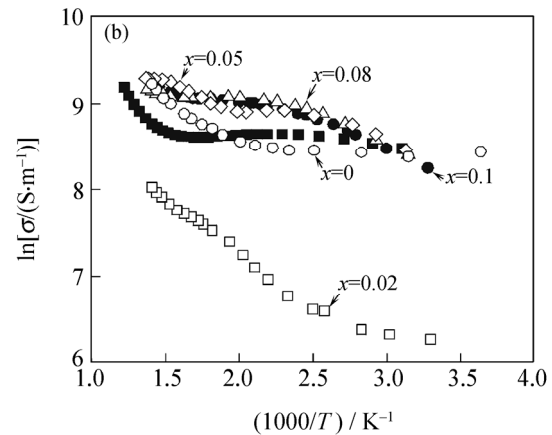


Fig. 3. Temperature dependence of electrical conductivity for  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$  (a) and the relationship between  $\ln\sigma$  and  $1000/T$  (b).

Table 1. Calculated  $E_g$  values of  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$

$x$	0	0.02	0.05	0.08	0.10	0.20
$E_g / \text{eV}$	0.58	0.44	0.35	0.37	0.39	0.62

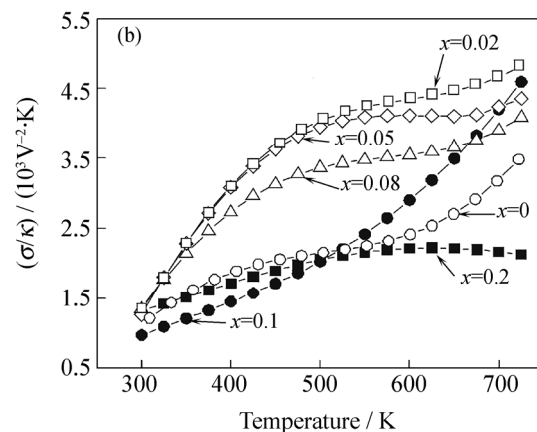
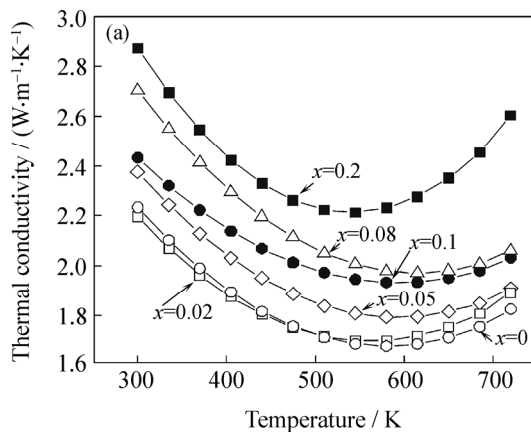


Fig. 4. Temperature dependences of thermal conductivity (a) and  $\sigma/\kappa$  (b) for  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$ .

Fig. 5 shows the dimensionless figure of merit  $ZT$  of all the samples against temperature.

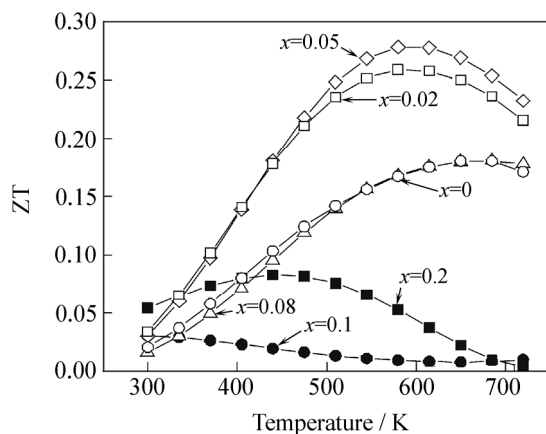


Fig. 5. Temperature dependence of the dimensionless figure of merit  $ZT$  for  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$ .

Because of the higher electrical conductivities and lower thermal conductivities of  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.55}\text{Ge}_{0.05}$  and  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.58}\text{Ge}_{0.02}$ , the  $ZT$  values of these samples exceed those of other ones. The maximum  $ZT$  value of  $\sim 0.28$  at about 550 K is obtained for  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.55}\text{Ge}_{0.05}$ .

#### 4. Conclusion

Thermoelectric properties of the quaternary system  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.6-x}\text{Ge}_x$  prepared by induction melting followed by hot-pressing were evaluated. XRD patterns revealed that all the compacts contained multiple phases. The maximum Seebeck coefficient and electrical conductivity were measured to be about  $325 \mu\text{V}\cdot\text{K}^{-1}$  for p-type and  $-350 \mu\text{V}\cdot\text{K}^{-1}$  for n-type and over  $11000 \text{ S}\cdot\text{m}^{-1}$ , respectively.  $\sigma/\kappa$  increases after

adding Ge though a higher lattice thermal conductivity was obtained. The maximum ZT value was about 0.28 for  $\text{Mg}_2\text{Sn}_{0.4}\text{Si}_{0.55}\text{Ge}_{0.05}$ .

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