

# FRACTAL STRUCTURE OF THE CORE LOSS SPECTRUM OF SOFT MAGNETIC ALLOY WITH CONSTANT PERMEABILITY

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**ABSTRACT** The core loss spectrum  $P(f)$  of magnetic alloy with constant permeability has been studied. It is found that  $P(f)$  has the fractal structure. The effect of the induced anisotropy energy  $K_u$  on the fractal dimension  $D_f$  is discussed.

**KEY WORDS** magnetic alloy with constant permeability, core loss, fractal

1J66, 1J34H and 1J34KH soft magnetic alloys are low residual magnetization materials originally created in China. Having constant permeability within a certain range of magnetized field, they are crucial materials used to make induction device. Because they work under the conditions of rather high frequency and magnetic induction  $B_m$ , the total power loss  $P$  is an important index to evaluate their magnetic properties. Generally,  $P$  increases with the increasing frequency, thus the frequency character of  $P(f)$  directly affects both the stability of permeability and quality factor  $Q$ . Traditionally, the total power loss spectrum  $P(f)$  is given by following formula [1]:

$$P(f) = P_e + P_h + P_c = eB_m^2 f^2 + \eta B_m^{1.6} f + P_c \quad (1)$$

where  $P_e = eB_m^2 f^2$  is the eddy-current loss,  $P_h = \eta B_m^{1.6} f$  is the magnetic hysteresis loss and  $P_c$  is the residual loss. Through an assumed physical model of technology magnetization, the loss coefficients  $e$  and  $\eta$  can be calculated by using specific material's properties (electric resistivity and thickness, etc.) and magnetic domain structure.

Many experimental results, however, have proven that formula (1) is not suitable to high permeability soft magnetic alloys at high frequency. Their total loss per cycle  $P(f)/f$  is not linear with  $f$ , and  $P(f)$  can not be simply separated according to (1). In this paper, the loss spectrum  $P(f)$  of three soft magnetic alloys with constant permeability (1J66, 1J34H and 1J34KH) has been investigated in a high frequency range as  $B_m = 0.1T$ . It is found that  $P(f)$  has a typical fractal structure [2]. This result confirms the fact that the fractal formula of  $P(f)$ , proposed by the author in another paper regarding the rectangular loop soft magnetic alloy, is suitable to the constant permeability alloy as well. Furthermore, the influence of the anisotropy energy  $K_u$ , induced by transverse magnetic heat treatment, on the fractal dimension of  $P(f)$  is discussed.

# 1 SPECIMENS AND MAGNETIC MEASUREMENTS

Three constant permeability alloys have been studied. Specimen A is 1J66 alloy ( Ni65Mn1Fe34 ), specimen B is 1J34H alloy ( Ni34Co39Mo3Fe24) and specimen C is 1J34KH ( Ni34Co39Mo3Nb3Fe21). After certain high temperature and transverse magnetic field heat treatments, the induced uniaxial anisotropy is produced in the specimens so that the low residual magnetization and constant permeability are obtained. The specimens are ring core with 16 mm in internal diameter and 26 mm in external diameter. The thin sheet used to make the core is 0.05 mm in thickness and 10 mm in width. The anisotropy energy  $K_u$  and D. C. magnetic properties were measured by magnetization work and ballistic methods respectively. The total power loss  $P(f)$  and dynamic permeability as  $B_m=0.1T$  were tested with a transformer-bridge.

## 2 RESULTS AND DISCUSSIONS

### 2.1 FRACTAL FORMULA OF LOSS SPECTRUM $P(f)$

Table 1 lists the  $P(f)$  data of specimen A, B and C measured as  $B_m=0.1T$ .

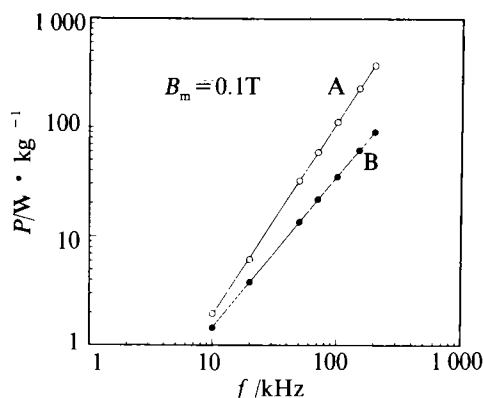
If  $\log P(f)$  is plotted as a function of  $\log f$ , the three curves are all straight lines, which is the typical character reflecting the fractal structure of  $P(f)$ . Both curves of specimens A and B are illustrated in Fig.1. The curve of specimen C is similar to those of specimens A and B.

Fig.1 shows that within the non-scale frequency range from 10 kHz to 200 kHz, the loss spectrum  $P(f)$  of the three constant permeability alloys has fractal structure.  $P(f)$  can be unitedly given by following fractal formula:

$$P(f) = P_0 f^{D_f} \tag{2}$$

**Table 1 Total power loss  $P(f)$  of specimen A, B and C ( $B_m=0.1T$ )**

$f$ /kHz	$P/W \cdot \text{kg}^{-1}$		
	A	B	C
10	1.95	1.45	4.10
20	6.17	3.80	10.20
50	32.20	13.50	33.90
70	59.10	21.70	51.90
100	112.00	35.00	85.00
150	227.00	61.80	144.00
200	369.00	90.60	297.00



**Fig. 1  $\log P(f)$  vs  $\log f$  curves of A and B**

where  $D_f$ , generally a fraction, is the fractal dimension of the loss spectrum and  $P_0$  is a constant. Both  $D_f$  and  $P_0$  are related to the intrinsic properties of materials and heat treatment technology conditions. The values of  $D_f$ ,  $P_0$ , anisotropy energy  $K_u$  and permeability  $\mu$  are given in table 2.

The value of the fractal dimension  $D_f$  is really a fraction (see table 2). Its meaning, describing the fractal structure, differs from that of integral numbers 2

Table 2  $D_f$ ,  $P_0$ ,  $K_u$  and  $\mu$  of the specimens

Specimen	$D_f$	$P_0, \times 10^6$	$K_u/J \cdot m^{-3}$	$\mu$	Constant range $/A \cdot m^{-1}$
A	1.76	0.17	17.50	2 880	0 ~ 240
B	1.38	4.43	61.90	1 170	0 ~ 796
C	1.31	24.30	119.60	616	0 ~ 1 194

and 1 appearing in the traditional eddy-current loss  $P_e \propto f^2$  and magnetic hysteresis loss  $P_h \propto f^1$  formulas respectively.  $D_f$  indicates the character—the total loss, caused by various mechanisms (such as eddy-current, magnetic hysteresis, relaxation, etc.), increases with the increasing frequency. The larger  $D_f$  is, the worse the frequency character of  $P(f)$  is.

## 2.2 A COMPARISON BETWEEN TWO FORMULAE OF $P(f)$

For specimen A, the fractal formula of loss spectrum can be written as :

$$P(f) = 1.73 \times 10^{-7} f^{1.76} \quad (\text{W/kg}) \quad (3)$$

The traditional  $P(f)$  formula can be obtained with very high confidence level according to the formula (1). It is:

$$P(f) = 7.13 \times 10^{-9} f^2 + 45.69 \times 10^{-5} f - 5.71 \quad (\text{W/kg}) \quad (4)$$

Through (3) and (4), the value of  $P$  can be calculated (listed in table 3).

From the comparison and table 3, it is found that the value of  $P(f)$  calculated using both formulae agrees with the observed value well. However, the value of residual loss in traditional formula is negative, which is difficult to explain in physics. The fractal formula has no such difficulty. Moreover the fractal formula agrees with the observed  $P(f)$  better than the tra-

Table 3 A comparison between two formulae of  $P(f)$ 

$f/\text{kHz}$	$P/\text{W} \cdot \text{kg}^{-1}$		
	Observed	Formula(3)	Formula(4)
10	1.95	1.90	-0.43
20	6.17	6.41	6.28
50	32.20	32.21	34.96
70	59.10	58.21	61.21
100	112.00	109.16	111.28
150	227.00	222.31	223.25
200	369.00	369.01	370.87

ditional one at the whole frequency range of 10 kHz ~ 200 kHz.

The conclusions of above comparison are applicable to specimens B and C, in which the fractal formulae are also superior to the traditional ones in describing loss spectrum.

In addition, above comparison illustrates that the fractal dimension  $D_f$  can represent qualitatively the ratio of eddy-current loss  $P_e$  to magnetic hysteresis loss  $P_h$  at a certain frequency. Taking specimen A as an example. For specimen A,  $D_f$  equals 1.76 and is close to 2 which appears in traditional eddy-current loss  $P_e \propto f^2$ . Using formula (4), the ratio of  $P_e$  to  $P_h$  can be calculated.  $P_e/P_h = 0.78$  as  $f = 50$  kHz,  $P_e/P_h = 1.56$  when  $f = 100$  kHz, and  $P_e/P_h = 3.12$  while  $f$  rises to 200 kHz. Comparatively, for specimens B and C, the value of  $D_f$  decreases to 1.38 and 1.31 respectively, and the value of  $P_e/P_h$  at a same frequency also decreases. Both  $D_f$  and  $P_e/P_h$  of the specimens are shown in table 4.

Table 4 shows that in specimen A (1J66 alloy), which has high  $\mu$  and narrow constant range, when  $f > 70$  kHz,  $P_e$  is greater than  $P_h$ . While in specimen B (1J34H

Table 4  $D_f$  and  $P_e/P_h$  of three specimens

Specimen	$D_f$	$P_e/P_h$				
		50 kHz	70 kHz	100 kHz	150 kHz	200 kHz
A	1.76	0.78	1.09	1.56	2.34	3.12
B	1.38	0.29	0.41	0.58	0.87	1.16
C	1.31	0.10	0.15	0.21	0.32	0.42

alloy), the frequency must be higher than 200kHz when  $P_e$  surpasses  $P_h$ . In specimen C (1J34KH alloy), which has the least  $\mu$  and widest constant range among three specimens,  $P_h$  is much greater than  $P_e$  at the whole frequency range from 10 kHz to 200 kHz.

As discussed in sections 2.1 and 2.2, the fractal formula of  $P(f)$  can excellently describe the behavior of total power loss in constant permeability alloys. The fractal dimension  $D_f$  can indicate the frequency character of  $P(f)$  and the ratio of eddy-current loss to magnetic hysteresis loss. The fractal formula is very simple and only uses two factors  $P_0$  and  $D_f$ , which are easy to measure. We suggest that it be reasonable to use fractal formula rather than traditional separation formula to describe the loss spectrum.

### 2.3 THE INFLUENCE OF INDUCED ANISOTROPY ENERGY $K_u$ ON BOTH $D_f$ AND $P_0$

By transverse magnetic heat treatment, the induced anisotropy will be produced in constant permeability alloys. Since the procedure of magnetization is mainly the rotation of magnetic domain and  $\mu \propto B_s^2/K_u$ , the general methods to develop constant permeability alloys are to determine saturation magnetic induction  $B_s$  by selecting the components of the alloy and to obtain appropriate value of  $K_u$  by searching for transverse magnetic heat treatment conditions. Through above methods, a constant permeability will be obtained at a certain range of magnetized field. It must be pointed out that  $K_u$  not only directly affects  $\mu$ , but also makes a great impact on both the fractal dimension  $D_f$  and factor  $P_0$ . The curves of  $D_f$  and  $P_0$  vs  $K_u$  are diagrammed in Fig. 2.

With the decrease of  $K_u$ ,  $D_f$  rises rapidly (see Fig.2). Though  $\mu$  increases with the decreasing  $K_u$ , the loss behavior becomes worse. This is the reason that it is hard to develop low loss alloys with high constant permeability in practice.

Also Fig. 2 shows that  $P_0$  drops sharply with the decrease of  $K_u$ . Since  $P(f)$  is determined by both  $P_0$  and  $D_f$ , specimen B, whose  $P_0$  is not so greater and  $D_f$  is smaller in value, has the least core loss among the three specimens.

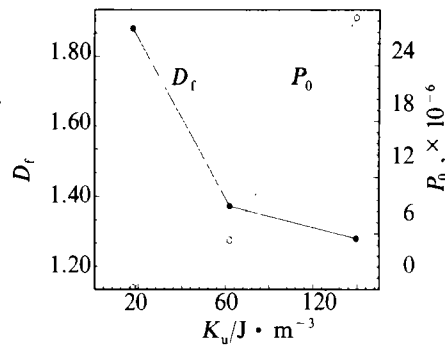


Fig. 2 Dependence of  $D_f$  and  $P_0$  on  $K_u$  in constant permeability alloys

### 3 CONCLUSIONS

- (1) Within the high frequency range from 10 kHz to 200 kHz, the loss spectrum  $P(f)$  of the three constant permeability alloys, 1J66, 1J34H and 1J34KH, has fractal structure  $P(f) = P_0 f^{D_f}$ , here  $D_f$  is its fractal dimension.
- (2) In these alloys, with the decrease of anisotropy energy  $K_u$ , permeability  $\mu$  increases, constant range becomes narrow, fractal dimension  $D_f$  rises rapidly and  $P_0$  drops greatly. By controlling the value of  $K_u$ , the constant permeability alloy with low core loss can be developed.
- (3) In the 10kHz ~ 200kHz frequency range, the value of  $D_f$  is able to indicate qualitatively the ratio of eddy-current loss to magnetic hysteresis loss.

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## 恒导磁合金损耗谱的分形结构

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**摘要** 研究了恒导磁合金的铁芯损耗谱  $P(f)$ , 发现  $P(f)$  具有分形结构. 讨论了感生各向异性性能  $K_u$  对分形维数  $D_f$  的影响.

**关键词** 恒导磁合金, 铁芯损耗, 分形